UCD Mat 67: Linear Algebra

This class may well be one of your first mathematics classes that bridges the gap between the mainly computation-oriented lower division classes and the abstract mathematics encountered in more advanced mathematics courses. The goal of this class is threefold:

1. You will learn Linear Algebra, which is one of the most widely used mathematical theories around. Linear Algebra finds applications in virtually every area of mathematics, including Multivariate Calculus, Differential Equations, and Probability Theory. It is also widely applied in fields like physics, chemistry, economics, psychology, and engineering. You are even relying on methods from Linear Algebra every time you use an Internet search like Google, the Global Positioning System (GPS), or a cellphone.

2. You will acquire computational skills to solve linear systems of equations, perform operations on matrices, calculate eigenvalues, and find determinants of matrices.

3. In the setting of Linear Algebra, you will be introduced to abstraction. We will develop the theory of Linear Algebra together, and you will learn to write proofs.

The lectures will mainly develop the theory of Linear Algebra, and the discussion sessions will focus on the computational aspects. The lectures and the discussion sections go hand in hand, and it is important that you attend both. The exercises for each Chapter are divided into more computation-oriented exercises and exercises that focus on proof-writing.

Linear Algebra is the branch of mathematics aimed at solving systems of linear equations with a finite number of unknowns.
1. What is linear algebra

2. Introduction to complex numbers

\[ g(x) = \int_{a}^{x} f(t) \, dt \]

3. The fundamental theorem of algebra and factoring polynomials

4. Vector spaces

5. Span and Bases
6. Linear Maps

\[ T = \begin{bmatrix} T_{11} & T_{12} \\ 0 & T_{22} \end{bmatrix} \]

7. Eigenvalues and eigenvectors

8. Permutations and the determinant

9. Inner product spaces

10. Change of bases

\[ A = \int_{\sigma(A)} \lambda \, dE_\lambda \]

11. The Spectral Theorem for normal linear maps

12. Supplementary notes on matrices and linear systems
13. Appendices

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Both hardbound and softbound versions of this textbook are available online at WorldScientific.com.